Minimum Magnitude of Completeness in Earthquake Catalogs: Examples from Alaska, the Western United States, and Japan

by Stefan Wiemer and Max Wyss

Abstract We mapped the minimum magnitude of complete reporting, $M_c$, for Alaska, the western United States, and for the JUNEC earthquake catalog of Japan. $M_c$ was estimated based on its departure from the linear frequency-magnitude relation of the 250 closest earthquakes to grid nodes, spaced 10 km apart. In all catalogs studied, $M_c$ was strongly heterogeneous. In offshore areas the $M_c$ was typically one unit of magnitude higher than onshore. On land also, $M_c$ can vary by one order of magnitude over distance less than 50 km. We recommend that seismicity studies that depend on complete sets of small earthquakes should be limited to areas with similar $M_c$, or the minimum magnitude for the analysis has to be raised to the highest common value of $M_c$. We believe that the data quality, as reflected by the $M_c$ level, should be used to define the spatial extent of seismicity studies where $M_c$ plays a role. The method we use calculates the goodness of fit between a power law fit to the data and the observed frequency-magnitude distribution as a function of a lower cutoff of the magnitude data. $M_c$ is defined as the magnitude at which 90% of the data can be modeled by a power law fit. $M_c$ in the 1990s is approximately $1.2 \pm 0.4$ in most parts of California, $1.8 \pm 0.4$ in most of Alaska (Aleutians and Panhandle excluded), and at a higher level in the JUNEC catalog for Japan. Various sources, such as explosions and earthquake families beneath volcanoes, can lead to distributions that cannot be fit well by power laws. For the Hokkaido region we demonstrate how neglecting the spatial variability of $M_c$ can lead to erroneous assumptions about deviations from self-similarity of earthquake scaling.

Introduction

The minimum magnitude of complete recording, $M_c$, is an important parameter for most studies related to seismicity. It is well known that $M_c$ changes with time in most catalogs, usually decreasing, because the number of seismographs increases and the methods of analysis improve. However, differences of $M_c$ as a function of space are generally ignored, although these, and the reasons for them, are just as obvious. For example, catalogs for offshore regions, as well as regions outside outer margins of the networks, are so radically different in their reporting of earthquakes that they should not be used in quantitative studies together with the catalogs for the central areas covered.

In seismicity studies, it is frequently necessary to use the maximum number of events available for high-quality results. This objective is undermined if one uses a single overall $M_c$ cutoff that is high, in order to guarantee completeness. Here we show how a simple spatial mapping of the frequency-magnitude distribution (FMD) and application of a localized $M_c$ cut-off can assist substantially in seismicity studies. We demonstrate the benefits of spatial mapping of $M_c$ for a number of case studies at a variety of scales.

For investigations of seismic quiescence and the frequency-magnitude relationship, we routinely map the minimum magnitude of completeness to define an area of uniform reporting for study (Wyss and Martyrosian, 1998, Wyss et al., 1999). Areas of inferior reporting (higher $M_c$), outside such a core area, are excluded because these data would contaminate the analysis. In seismicity studies where statistical considerations play a key role, it is important that results are not influenced by the choice of the data limits. If these limits are based on the catalog quality, then improved statistical robustness may be assured. For this reason we routinely map the quality of the catalog for selecting the data for our studies of seismic quiescence; however, homogeneity in $M_c$ does not necessarily guarantee homogeneity in earthquake reporting, since changes in magnitude reporting influence the magnitude of homogeneous reporting (Habermann, 1986; Habermann, 1991; Zuniga and Wyss, 1995; Zuniga and Wiemer, 1999).

Our estimation of $M_c$ is based on the assumption that, for a given, volume a simple power law can approximate the FMD. The FMD (Ishimoto and Iida, 1939; Gutenberg and
Richter, 1944) describes the relationship between the frequency of occurrence and magnitude of earthquakes:

$$\log_{10} N = a - bM,$$  \hspace{1cm} (1)

where $N$ is the cumulative number of earthquakes having magnitudes larger than $M$, and $a$ and $b$ are constants. Various methods have been suggested to measure $b$ and its confidence limits (Aki, 1965; Utsu, 1965, 1992; Bender, 1983; Shi and Bolt, 1982; Frohlich and Davis, 1993). The FMD has been shown to be scale invariant down to a source length of about 10 m (Abercrombie and Brune, 1994) or approximately magnitude 0 event size. Some authors have suggested changes in scaling at the higher magnitude end (e.g., Lomnitz-Adler and Lomnitz 1979; Utsu, 1999) or for smaller events (Aki, 1987). However, neither of these suggested changes in slope will be relevant for the estimate of $M_c$ because by far the dominant factor changing the slope of the FMD is incompleteness in reporting for smaller magnitudes. In Figure 1 we show the overall FMD in cumulative (Figure 1a) and noncumulative (Figure 1b) form for the three data sets we investigate. We assume that the drop in the number of events below $M_c$ is caused by incomplete reporting of events.

Other studies that have addressed the completeness problem have either used changes between the day and nighttime sensitivity of networks (Rydelek and Sacks, 1989, 1992), comparison of amplitude-distance curves and the signal-to-noise ratio (Sereno and Bratt, 1989; Harvey and Hansen, 1994) or amplitude threshold studies (Gomberg, 1991) to estimate $M_c$. Waveform-based methods that require estimating the signal-to-noise ratio for numerous events at many stations are time-consuming and cannot generally be performed as part of a particular seismicity study. Using the FMD to estimate completeness is probably the simplest method. Our study demonstrates that despite some obvious shortcomings, spatially mapping of $M_c$ based on the FMD is a quick yet useful tool for seismicity analysis and should in our opinion be a routine part of seismicity related studies.

**Method**

The first step toward understanding the characteristics of an earthquake catalog is to discover the starting time of the high-quality catalog most suitable for analysis. In addition, we seek to identify changes of reporting quality as a function of time. Issues connected with these problems are not the subjects of this article; they are dealt with elsewhere (Habermann, 1986; Habermann, 1991; Zuniga and Wiemer, 1999; Zuniga and Wyss, 1995). Here we assume that we know the starting date of the high-quality catalog, and that there are no changes of reporting (magnitude stretches and shifts) serious enough to corrupt the analysis we have in mind, so that we may proceed to map $M_c$.

Our estimate of $M_c$ is based on the assumption of a Gutenberg-Richter (GR) power law distribution of magnitudes (equation 1). To evaluate the goodness of fit, we compute the difference between the observed FMD and a synthetic distribution. For incomplete data sets, a simple power law cannot adequately explain the observed FMD, so the difference will be high.

The following steps are taken to estimate $M_c$: First we estimate the $b$- and $a$-value of the GR law as a function of minimum magnitude, based on the events with $M \geq M_i$. We use a maximum likelihood estimate to estimate the $b$- and $a$-values and their confidence limits (Aki, 1965; Shi and Bolt, 1982; Bender, 1983). Next, we compute a synthetic distribution of magnitudes with the same $b$-, $a$- and $M_i$ values, which represents a perfect fit to a power law. To estimate the goodness of the fit we compute the absolute difference, $R$, of the number of events in each magnitude bin between the observed and synthetic distribution.
where $B_i$ and $S_i$ are the observed and predicted cumulative number of events in each magnitude bin. We divide by the total number of observed events to normalize the distribution. Our approach is illustrated in Figure 2, which shows $R$ as function of $M_i$. If $M_i$ is smaller then the ‘correct’ $M_c$, the synthetic distribution based on a simple power law (squares in Figure 2) cannot model the FMD adequately and, consequently, the goodness of fit, measured in percent of the total number of events, is poor. The goodness-of-fit value $R$ increases with increasing $M_i$ and reaches a maximum value of $R \sim 96\%$ at $M_c = 1.8$ in this example. At this $M_c$, a simple power law with the assumed $b$-, $a$-, and $M_c$ value can explain 96% of the data variability. Beyond $M_i = 1.8$, $R$ increases again gradually. In this study we map $M_c$ at the 90% level, that is, we define $M_c$ as the point at which a power law can model 90% or more of the FMD. For the example shown in Figure 2, we therefore define $M_c = 1.5$. Not all FMDs will reach the 90% mark. In some cases the FMDs are too curved or bimodal to be fitted satisfactory by a simple power law. This can be due to strong spatial or temporal inhomogeneities in the particular sample, or actual physical processes within the earth. An example of the former would be a drastic change of the completeness of recording during the investigated period; an example of the latter might be a volcanic region where distinct earthquake families and swarms are frequent. It is important to identify these areas for studies of the FMD, because here a power law cannot be readily applied. Our method allows us to map the fit to a power law behavior at each node, based on the minimum value of $R$ obtained.

For mapping $M_c$, we use the gridding technique applied in our studies of $b$-values and seismic quiescence (Wiemer and Wyss, 1997; Wiemer et al., 1998; Wiemer and Katsumata, 1999). Grids with several thousand nodes spaced regularly at 1 to 20 km distances, depending on the size of the area to be covered, the density of earthquakes, and the computer power available, are arbitrarily placed over the study region, and we construct the FMD at each node for the $N$ nearest events and estimate $M_c$ using the approach outlined previously. At the same time, we compute a map of the goodness of fit to a power law by finding the minimum $R$ from equation (2) at each node. The same type of spatial

$$R(a, b, M_c) = 100 - \left( \frac{\sum |B_i - S_i|}{\sum B_i} \right)$$

Figure 2. Explanation of the method by which we estimated the minimum magnitude of completeness, $M_c$. The three frames at the top show synthetic fits to the observed catalog for three different minimum magnitude cutoffs. The bottom frame shows the goodness of fit $R$, the difference between the observed and a synthetic FMD (equation 2), as a function of lower magnitude cut-off. Numbers correspond to the examples in the top row. The $M_c$ selected is the magnitude at which 90% of the observed data are modeled by a straight line fit.
gridding can also be applied in cross sections (e.g., Wiemer and Benoit, 1996; Power et al., 1998).

Data and Observations

In the following section, we apply the spatial mapping of $M_c$ to three test cases: Alaska, Western United States, and Japan.

Alaska

The seismicity catalog compiled by the Alaska Earthquake Information Center (AEIC) for the period of January 1992–December 1998 contains a total of about 21,000 events for central and interior Alaska with a depth less than 60 km and $M > 0.5$. An epicenter map also identifying the main faults is shown in Figure 3c. We mapped $M_c$ using a sample size of $N = 250$ and a node spacing of 10 km. The grid we created excludes low-seismicity areas. The sampling radii are typically $r = 70$ km, and none are larger than 200 km. $M_c$ varies from values near 1.4 in the interior, near Fairbanks, and in the south, between Anchorage and Valdez (blue/purple in Figure 3a), to values of $M_c > 3$ offshore and on Kodiak Island (red in Figure 3a). In Figure 4a we show a comparison of the FMDs for three areas: The vicinity of Fairbanks ($M_c \sim 1.4$), the Mt. McKinley area ($M_c \sim 2.1$), and Kodiak Island ($M_c \sim 3.3$).

A map of the goodness of fit to a GR distribution is shown in Figure 3b. Mapped is the parameter $R$; low $R$-values ($R < 90\%$), shown in hot colors indicate that only a poor fit to a GR distribution could be obtained. Several areas can be identified where the best fitting GR explains less than 90\% of the observed distribution. The poorest fit to a GR distribution is...
law \((R < 80\%)\) can be observed near the volcanoes Mt. Spurr and Mt. Redoubt. In this area, the observed FMD (Figure 4b) is bimodal; two different populations of events are contained in the sample.

### Western United States

We used the seismicity catalog compiled by the Council of the National Seismic Systems (CNSS) for the period of January 1995–May 1999 and events with a depths less than 30 km. Figure 5c shows the epicenter map of the area investigated. The spatial distribution of \(M_c\) is plotted in Figure 5a. The goodness-of-fit map (Figure 5b) indicates numerous small regions where the fit to GR is less than 90% satisfactory.

### Southern California

Off-shore (Figures 4c and 5a) the resolution is not as good \((M_c \approx 2 \pm 0.2)\) as it is on land and within the network, where \(M_c < 1.7\) in most parts, except for the Mojave Desert (Figure 5a). The best resolution \((M_c \approx 0.8)\) is achieved in the less populated Landers (Figures 4c and 5a), Salton Sea, San Jacinto, and Malibu areas. Pt. Conception, west of Santa Barbara, seems to be poorly covered \((M_c \approx 2.0)\). In the Los Angeles area a resolution of \(M_c \approx 1.5\) is achieved, which is remarkable, given the industrial noise level.

### Northern California

The poorest coverage with \(M_c > 2.7\) is seen far off the coast off Cape Mendocino (Figures 4e and 5a). At Cape Mendocino itself, \(M_c \approx 2\). Most of the seismicity in the San Andreas fault system (west of the Great Valley) is resolved at levels of \(M_c < 1.6\). The best job \((M_c \approx 0.8)\) is achieved south of the San Francisco Bay to Parkfield (Figures 4e and 5a) and in the Mammoth Lake area. The border region with Nevada is not well covered; \(M_c\) rises above the 2.3 level in places. \(M_c\) also increases to \(-2\) at the boundary between the northern and southern California seismic networks, south of Parkfield.

### Japan

Our analysis is based on the Japan University Network (JUNEC) catalog for the period of January 1986–December 1990. Japan is covered by regional seismograph networks, which are run separately by universities and government research laboratories. JUNEC combined these data in a single catalog. The epicenter map for earthquakes with depths shallower than 35 km is shown in Figure 6c, the spatial distribution of \(M_c\) is imaged in Figure 6a. The \(M_c\) in the subducting slab beneath central Japan is shown in Figure 7.

In this catalog the seismicity located farther than about 100 km offshore is resolved only above the \(M_c \approx 3.2\) level (Figure 6a). Within approximately 100 km from the coast, the completeness magnitude varies between 2.5 and 2.8. The areas in central Japan, near Tokyo and near Kyoto show the lowest \(M_c\) of about 1.3, whereas in northern Japan, \(M_c \approx 2.4\) in this catalog.

The cross-sectional analysis in the Kanto region, central Japan (Figure 7) reveals the lowest \(M_c\) level \((M_c \approx 2.0)\) onshore. With increasing distance from land, \(M_c\) increases gradually to values greater than 3. Deep earthquakes in the subducting plate show a \(M_c \approx 3\) at 200 km depth, and \(M_c \approx 3.5\) at 400-km depth.

This analysis does not represent the full extent of information available on seismicity in Japan. The catalogs of individual organizations such as Bosai and Tohoku University, for example, resolve the areas covered by their networks to significantly lower magnitudes than the JUNEC catalog does. However, since the JUNEC catalog is readily available, and because it covers all of Japan, the variations of \(M_c\) in it are of interest.
Discussion and Conclusions

Spatially Mapping $M_c$

The magnitude of completeness varies spatially throughout all seismic networks. By assessing the goodness of fit to a power law, we can reliably and quickly map out the spatial variability of $M_c$, based purely on catalog data. A solid knowledge of $M_c$ is important for many seismicity and probabilistic earthquake hazard studies, and we propose that spatially mapping $M_c$ should be performed routinely as part of seismicity studies. (The software used in this study can be freely downloaded as part of the ZMAP seismicity analysis package; http://www.seismo.ethz.ch/staff/stefan). Knowing the spatial distribution of $M_c$ is important for regional studies that use bulk $b$-values. By excluding high $M_c$ areas, the magnitude threshold for analysis can be lowered and the amount of data available for analysis increased. For studies that address the spatial variability of the FMD, knowledge of the spatial distribution of $M_c$ is imperative.

From the $M_c$ maps (Figures 3, 5, and 6) we see that in most of Alaska the seismicity is resolved to $M_c = 1.8 \pm 0.4$, in most of California the completeness level is at $M_c = 1.2 \pm 0.4$, and in the JUNEC catalog of Japan it is not better than in Alaska. In the Aleutian islands of Alaska, the seis-
Figure 6. (a) Map of Japan. Color-coded is the minimum magnitude of completeness, $M_c$, estimated from the nearest 250 earthquakes to nodes of a grid spaced 10 km apart. The typical sampling radii are $r = 62$ km, and all $r < 150$ km. (b) Map of the local goodness of fit of a straight line to the observed frequency-magnitude relation as measured by the parameter $R$ in percent of the data modeled correctly. (c) Epicenters of earthquakes in Japan for the period 1986–1992 and depth $< 35$ km.

At the levels of completeness seen in California, faults can be mapped quite well, as one can see in the epicenter maps of Figures 5c. However, at the somewhat higher levels of completeness in Alaska it becomes more difficult to map faults (Fig. 3a). In Japan the level of completeness shown by the JUNEC catalog is not considered adequate. Not only do regional networks furnish lower $M_c$ values, but also Japan has undertaken a new, strong push to install many more seismographs to monitor the seismicity in much greater detail.

We investigated the correlation between the density of seismic stations and the magnitude of completeness. At each node of the $M_c$ grid for California (Fig. 5) and Alaska (Fig. 3), we find the distance in kilometers of the 4th closest station to this node. Since four stations are the minimum number required to obtain a hypocenter solution, this distance is one possible measure of the local density of stations. For this simple approximation we only consider vertical channels. Results are shown in Figure 8a for California and 8b for Alaska. As expected, $M_c$ increases systematically with in-

mically most active part of the United States, the $M_c$ exceeds that of the SW corner of Kodiak island, where $M_c = 3.4$. For the CNSS catalog, event data are merged rather than the phase data, before relocation with the combined set. Thus events near network boundaries are detected and located from one network only. This is consistent with the increase in $M_c$ we see near CNSS network boundaries (Fig. 5).

Heterogeneity of the $M_c$ is considerable in some areas. $M_c$ can change by one full magnitude unit over distances of less than 50 km. Some of these cases may be known to the network operators and determined to be acceptable; others may not be known and could possibly be reviewed. For example, it may not be desirable to have a relatively high $M_c$ along the coast west of Santa Barbara, whereas an improvement of the resolution to lower $M_c$ values may not be economical in some places, like western and central Alaska. Analysis of $M_c$ as a function of space and time may help network operators to make decisions on an informed basis for improving their monitoring efforts.
creasing distance; however, the data show considerable spread and outliers. The curve for Alaska is systematically higher than the one for California; particularly for small $M_c$. We speculate that factors beyond station density, such as the ambient noise level at the sites, influence $M_c$; in Alaska the ambient noise due to human activity is lower than in highly populated California. These plots (Figure 8) can give network operators a rough estimate what decrease in $M_c$ might be possible through network densification.

In past studies (Wiemer and Katsumata, 1999; Wiemer and McNutt, 1997; Wyss et al., 2000) we have estimated $M_c$ using the point of maximum curvature of the FMD. This simpler measure delivers a good first estimate of $M_c$, however, it tends to underestimate $M_c$ in the case of gradually curved FMDs that are indicative of spatial and temporal heterogeneity of earthquake catalogs. A test for the Alaska data set shows that, averaged over all nodes, the difference in $M_c$ between the two methods is 0.13. However, differences at a few nodes can be as high as 0.5. We consider the presented measure of $M_c$ to be superior because it also identifies volumes in which a power law distribution of events cannot be assumed and because it applies a more quantitative criterion. Tests performed on the diverse data sets presented here have confirmed that the method to estimate $M_c$ introduced here is robust and reliable.

Estimating $M_c$ solely based on the FMD has some obvious drawbacks. For example, $M_c$ cannot be estimated in areas of low seismicity. Unlike methods based on the signal-to-noise ratio and amplitude-distance curves (Gomberg, 1991; Harvey and Hansen, 1994; Sereno and Bratt, 1989), our method cannot forecast the detection capability of a network, neither is it capable of forecasting $M_c$ based on hypothetical network configurations. It does, however, result in a reliable first-order approximation of the capabilities of seismic networks in the areas most interest: high-seismicity areas. The advantage of our method is that it can be performed easily, without requiring a time-consuming study of signal-to-noise ratio and amplitude-distance curves. Therefore, it can be applied as a routine part of any seismicity-related study.

Estimating $M_c$ based on the difference in day and nighttime sensitivity (Rydelek and Sacks, 1989, 1992) has the drawbacks that (1) large samplesizes are need to estimate $M_c$, thus seriously limiting the ability to spatially map $M_c$; (2) contamination through quarry blast exists; (3) the method cannot readily be applied in areas with low cultural noise, such as Alaska. However, unlike our approach, no assumption about the linearity of the FMD is made.

Non-Power Law Behavior

By assessing the goodness of fit to a power law, we can identify areas where the estimate of $M_c$ is likely to be inaccurate (Figs. 3b, 5b, 6b), that is, where $R < 90\%$. These areas deserve special attention in hazard and seismicity-related studies, because here extrapolations to larger magnitudes that are commonly done in probabilistic hazard as-

**Figure 7.** Cross-sectional view through the subducting Pacific plate in the Tohoku region, northern Japan. The top frame shows topography and bathymetry. The middle frame displays hypocenter location obtained from the JUNEC catalog for the period January 1986–December 1991. The bottom frame represents the distribution of $M_c$.

**Figure 8.** Plot of the distance to the 4th nearest station as a function of $M_c$. (Top) Based on the $M_c$ map for California (Fig. 5). (Bottom) Based on the $M_c$ map for Alaska (Fig. 3).
Minimum Magnitude of Completeness in Earthquake Catalogs: Examples from Alaska, the Western United States, and Japan

Figure 9. (a) Histogram of the hourly number of events south of Salt Lake City, Utah. The corresponding FMD is shown in Fig. 4d. The peak in the hourly distribution indicates that this region contains a large percentage of explosions, because many more events occur during the afternoon than at other times. (b) Histogram of the magnitudes for the same sample.

Figure 10. (a) Map of the southeastern tip of Hokkaido, Japan. Color-coded is the minimum magnitude of completeness, $M_c$, estimated from the nearest 250 earthquakes to nodes of a grid spaced 5 km apart. The triangle marks the location of station KMU; the circle indicates the volume analyzed by Rydelek and Sacks (1989) and Taylor et al. (1990). (b) Map of the local goodness of fit of a straight line to the observed frequency-magnitude relation as measured by the parameter $R$ in percent of the data modeled correctly. (c) Epicenters of earthquakes for the period 1986–1992 and depth <45 km.

Assessments must be considered less reliable. Volant and Scotti (1998) proposed to estimate the standard deviation of the $b$-value with a nonweighted least squares technique to quantify the departure from linearity in the tail of the FMD. Using this technique, they were able to map zones of nonlinear behavior in the Western Alps. It is not within this study to systematically investigate the cause of the non-power law behavior; however, for selected areas we demonstrate likely reasons.

The most outstanding non-power law curve in Alaska (Fig. 3a) is located near the volcanoes Mt. Spurr and Mt. Redoubt. Here, local dense networks are installed on the volcanoes, adding a population of small-magnitude events to the regional data set. This, and the possible inclusion of earthquake swarms and families common at volcanoes, result in a bimodal FMD as shown in Figure 4b that is the
telltale sign of combining populations of events with different properties.

In Utah we find low $R$-values south of Salt Lake City (Fig. 5b), and the respective FMD is shown in Figure 4d. In this region, we also notice a strong gradient in the $M_c$ values (Fig. 5a). In a plot of the hourly distribution of events for this volume (Fig. 9a), one notices a dominant peak during daytime hours, which is a telltale sign of blast activity (Wiemer and Baer, 2000). The combined FMD of the explosions that preferably scale around $M2$ (Fig. 9b) and natural earthquake results in a strongly nonlinear behavior of the FMD.

Rydelek and Sacks (1989) and Taylor et al. (1990) claim to have identified a deviation from the “common lore of linear $b$-values and the idea of the self-similar earthquake process” when analyzing crustal and deep events for the period 1977–1986 with 50 km of the station KMU, Hokkaido, Japan (143.0 E, 42.25 N). However, when analyzing the spatial variability of $M_c$ using the JUNEC catalog, based on the same network but for the period 1986–1992, we find a much simpler explanation of their observation: Within the sample volume ($R < 50$ km, depths $< 45$ km, black circle in Fig. 10a), $M_c$ varies drastically between onshore ($M_c \sim 1.8$) and offshore ($M_c \sim 2.5$) volumes. When mixing these different populations in one bulk analysis, a biased, low estimate of $M_c$ is obtained, leading to the erroneous claim that the FMD is not linear. To demonstrate this point, we plot in Figure 11 the FMD for the onshore (triangles) and offshore (squares) population, as well as the combined (circles) population. The offshore population clearly is not complete to values of $M_c \sim 1.8$ as assumed by Rydelek and Sacks (1989) and Taylor et al. (1990). Similar variability of $M_c$ between the deep and shallow earthquakes analyzed by Taylor et al. (1990) can be demonstrated, suggesting that in this case also the heterogeneity of $M_c$ caused the nonlinearity of the FMD.

We conclude that a careful estimate of the spatial and temporal homogeneity of $M_c$ is needed before any claim of deviations from a power law behavior for small magnitudes can be made. The daytime to nighttime activity variation criteria applied in Rydelek and Sacks (1989) and Taylor et al. (1990) do not seem able to determine $M_c$ correctly if $M_c$ varies spatially. The fraction of events to the SW of station KMU that requires a $M_c \sim 2.5$ (Fig. 10) does not make itself known in the phasor plots used by Rydelek and Sacks (1989) and Taylor et al. (1990).

Based on the examples listed previously and others we studied, we conclude that most non-power law FMDs are caused by (1) artifacts in the catalog, for example, changes in $M_c$ as a function of time; (2) mixing heterogeneous population of events, for example, explosions and tectonic earthquakes, or volcanic earthquake families and tectonic earthquakes; and (3) spatially heterogeneous $M_c$ distribution. We suspect that, after eliminating these so-called contaminations, most earthquake populations can be adequately described by a power law for a wide range of magnitudes.

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